

**User Manual and Source Code for a LAMMPS  
Implementation of Constant Energy Dissipative  
Particle Dynamics (DPD-E)**

**by James P. Larentzos, John K. Brennan, Joshua D. Moore, and  
William D. Mattson**

**ARL-SR-290**

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## **User Manual and Source Code for a LAMMPS Implementation of Constant Energy Dissipative Particle Dynamics (DPD-E)**

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14. ABSTRACT A user manual and source code files are provided for the implementation of the constant energy Dissipative Particle Dynamics method into the highly scalable Large-Scale Atomic/Molecular Massively Parallel Simulator (LAMMPS) simulation software. The current LAMMPS velocity-Verlet (VV) integration scheme is extended to model systems under isoenergetic cases. In addition, the Shardlow-splitting algorithm is provided as an alternative integration scheme that enables longer time steps with comparable accuracy to the VV integration scheme.					
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The constant energy dissipative particle dynamics (DPD-E) method is implemented into the Large-Scale Atomic/Molecular Massively Parallel Simulator (LAMMPS) simulation software to efficiently model systems under isoenergetic conditions using the current LAMMPS velocity-Verlet (VV) integration scheme and the Shardlow-splitting algorithm (SSA). The relevant source code files that are current with the 7 February 2014 release of LAMMPS are provided, along with the user manual documentation. The contents of this material are described in detail in U.S. Army Research Laboratory (ARL) technical report ARL-TR-6863.<sup>1</sup>

The DPD-E method using the VV and VV-SSA integration schemes has been implemented within LAMMPS as user packages under the directory src/USER-DPD in the accompanying compact disc (CD).

The LAMMPS user package USER-DPD can be added to the LAMMPS source files by issuing the command

```
make yes-USER-DPD
```

within the LAMMPS src/ directory. A copy of the modified user manual containing the new features added to LAMMPS can be found in the appendix, and the source txt, html, tex, and jpg files can be found within the LAMMPS doc/ and doc/Eqs directory in the accompanying CD. The full LAMMPS user manual can be found at <http://lammps.sandia.gov/doc/Manual.html>.

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<sup>1</sup> Larentzos, J. P.; Brennan, J. K.; Moore, J. D.; Mattson, W. D. *LAMMPS Implementation of Constant Energy Dissipative Particle Dynamics (DPE-E)*; ARL-TR-6863; U.S. Army Research Laboratory: Aberdeen Proving Ground, March 2014.

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**Appendix. Large-Scale Atomic/Molecular Massively Parallel Simulator  
(LAMMPS) User Manual for Commands Related to the Constant Energy  
Dissipative Particle Dynamics (DPD-E) Implementation With the Velocity-  
Verlet (VV) and VV-Shardlow-Splitting Algorithm (SSA) Integration  
Schemes**

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This appendix appears in its original form, without editorial change.

## atom\_style command

### Syntax:

```
atom_style style args
```

- *style* = *angle* or *atomic* or *body* or *bond* or *charge* or *dpd* or *dipole* or *electron* or *ellipsoid* or *full* or *line* or *meso* or *molecular* or *peri* or *sphere* or *tri* or *hybrid*

```
args = none for any style except body and hybrid
body args = bstyle bstyle-args
bstyle = style of body particles
bstyle-args = additional arguments specific to the bstyle
              see the body doc page for details
hybrid args = list of one or more sub-styles, each with their args
```

### Examples:

```
atom_style atomic
atom_style bond
atom_style full
atom_style body nparticle 2 10
atom_style hybrid charge bond
atom_style hybrid charge body nparticle 2 5
```

### Description:

Define what style of atoms to use in a simulation. This determines what attributes are associated with the atoms. This command must be used before a simulation is setup via a [read\\_data](#), [read\\_restart](#), or [create\\_box](#) command.

Once a style is assigned, it cannot be changed, so use a style general enough to encompass all attributes. E.g. with style *bond*, angular terms cannot be used or added later to the model. It is OK to use a style more general than needed, though it may be slightly inefficient.

The choice of style affects what quantities are stored by each atom, what quantities are communicated between processors to enable forces to be computed, and what quantities are listed in the data file read by the [read\\_data](#) command.

These are the additional attributes of each style and the typical kinds of physical systems they are used to model. All styles store coordinates, velocities, atom IDs and types. See the [read\\_data](#), [create\\_atoms](#), and [set](#) commands for info on how to set these various quantities.

<i>angle</i>	bonds and angles	bead-spring polymers with stiffness
<i>atomic</i>	only the default values	coarse-grain liquids, solids, metals
<i>body</i>	mass, inertia moments, quaternion, angular momentum	arbitrary bodies
<i>bond</i>	bonds	bead-spring polymers
<i>charge</i>	charge	atomic system with charges
<i>dpd</i>	internal temperature and energies	DPD particles

atom\_style command

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<i>dipole</i>	charge and dipole moment	system with dipolar particles
<i>electron</i>	charge and spin and eradius	electronic force field
<i>ellipsoid</i>	shape, quaternion, angular momentum	aspherical particles
<i>full</i>	molecular + charge	bio-molecules
<i>line</i>	end points, angular velocity	rigid bodies
<i>meso</i>	rho, e, cv	SPH particles
<i>molecular</i>	bonds, angles, dihedrals, impropers	uncharged molecules
<i>peri</i>	mass, volume	mesoscopic Peridynamic models
<i>sphere</i>	diameter, mass, angular velocity	granular models
<i>tri</i>	corner points, angular momentum	rigid bodies
<i>wavepacket</i>	charge, spin, eradius, etag, cs_re, cs_im	AWPMD

All of the styles define point particles, except the *sphere*, *ellipsoid*, *electron*, *peri*, *wavepacket*, *line*, *tri*, and *body* styles, which define finite-size particles. See [Section howto 14](#) for an overview of using finite-size particle models with LAMMPS.

All of the styles assign mass to particles on a per-type basis, using the `mass` command, except for the finite-size particle styles. They assign mass to individual particles on a per-particle basis.

For the *sphere* style, the particles are spheres and each stores a per-particle diameter and mass. If the diameter > 0.0, the particle is a finite-size sphere. If the diameter = 0.0, it is a point particle.

For the *ellipsoid* style, the particles are ellipsoids and each stores a flag which indicates whether it is a finite-size ellipsoid or a point particle. If it is an ellipsoid, it also stores a shape vector with the 3 diameters of the ellipsoid and a quaternion 4-vector with its orientation.

For the *electron* style, the particles representing electrons are 3d Gaussians with a specified position and bandwidth or uncertainty in position, which is represented by the `eradius` = electron size.

For the *peri* style, the particles are spherical and each stores a per-particle mass and volume.

The *meso* style is for smoothed particle hydrodynamics (SPH) particles which store a density (`rho`), energy (`e`), and heat capacity (`cv`).

The *dpd* style is for dissipative particle dynamics (DPD) particles which store the particle internal temperature (`dpdTheta`), internal conductive energy (`uCond`), internal mechanical energy (`uMech`), as well as other particle properties such as heat capacity (`cv`) and density (`rho`).

The *wavepacket* style is similar to *electron*, but the electrons may consist of several Gaussian wave packets, summed up with coefficients `cs= (cs_re,cs_im)`. Each of the wave packets is treated as a separate particle in LAMMPS, wave packets belonging to the same electron must have identical *etag* values.

For the *line* style, the particles are idealized line segments and each stores a per-particle mass and length and orientation (i.e. the end points of the line segment).

For the *tri* style, the particles are planar triangles and each stores a per-particle mass and size and orientation (i.e. the corner points of the triangle).

For the *body* style, the particles are arbitrary bodies with internal attributes defined by the "style" of the bodies, which is specified by the *bstyle* argument. Body particles can represent complex entities, such as surface meshes of discrete points, collections of sub-particles, deformable objects, etc.

The [body](#) doc page describes the body styles LAMMPS currently supports, and provides more details as to the kind of body particles they represent. For all styles, each body particle stores moments of inertia and a quaternion 4-vector, so that its orientation and position can be time integrated due to forces and torques.

Note that there may be additional arguments required along with the *bstyle* specification, in the *atom\_style* body command. These arguments are described in the [body](#) doc page.

---

Typically, simulations require only a single (non-hybrid) atom style. If some atoms in the simulation do not have all the properties defined by a particular style, use the simplest style that defines all the needed properties by any atom. For example, if some atoms in a simulation are charged, but others are not, use the *charge* style. If some atoms have bonds, but others do not, use the *bond* style.

The only scenario where the *hybrid* style is needed is if there is no single style which defines all needed properties of all atoms. For example, if you want dipolar particles which will rotate due to torque, you would need to use "atom\_style hybrid sphere dipole". When a hybrid style is used, atoms store and communicate the union of all quantities implied by the individual styles.

LAMMPS can be extended with new atom styles as well as new body styles; see [this section](#).

#### Restrictions:

This command cannot be used after the simulation box is defined by a [read\\_data](#) or [create\\_box](#) command.

The *angle*, *bond*, *full*, and *molecular* styles are part of the MOLECULAR package. The *line* and *tri* styles are part of the ASPHERE package. The *body* style is part of the BODY package. The *dipole* style is part of the DIPOLE package. The *peri* style is part of the PERI package for Peridynamics. The *electron* style is part of the USER-EFF package for [electronic force fields](#). The *dpd* style is part of the USER-DPDE and USER-DPDE-SHARDLOW packages for dissipative particle dynamics (DPD). The *meso* style is part of the USER-SPH package for smoothed particle hydrodynamics (SPH). See [this PDF guide](#) to using SPH in LAMMPS. The *wavepacket* style is part of the USER-AWPMD package for the [antisymmetrized wave packet MD method](#). They are only enabled if LAMMPS was built with that package. See the [Making LAMMPS](#) section for more info.

#### Related commands:

[read\\_data](#), [pair\\_style](#)

#### Default:

atom\_style atomic

## compute dpd command

### Syntax:

```
compute ID group-ID dpd
```

- ID, group-ID are documented in [compute](#) command
- dpd = style name of this compute command

### Examples:

```
compute 1 all dpd
```

### Description:

Define a computation that accumulates the total internal conductive energy (U\_cond), the total internal mechanical energy (U\_mech), the total internal energy (U) and the average internal temperature (Theta) of the entire system of particles. See the [compute dpd/atom](#) command if you want per-particle internal energies and internal temperatures.

The system internal properties are computed according to the following relations:

$$U^{cond} = \sum_{i=1}^N u_i^{cond}$$

$$U^{mech} = \sum_{i=1}^N u_i^{mech}$$

$$U = \sum_{i=1}^N (u_i^{cond} + u_i^{mech})$$

$$\theta_{avg} = \left( \frac{1}{N} \sum_{i=1}^N \frac{1}{\theta_i} \right)^{-1}$$

where N is the number of particles in the system

---

### Output info:

This compute calculates a global vector of length 4 (U\_cond, U\_mech, U, Theta), which can be accessed by indices 1-4. See [this section](#) for an overview of LAMMPS output options.

The vector values will be in energy and temperature [units](#).

### Restrictions:

The compute *dpd* is only available if LAMMPS is built with the appropriate USER-DPDE or

compute dpd command

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USER-DPDE-SHARDLOW package.

**Related commands:**

compute dpd/atom, thermo\_style

**Default:** none

---

**(Larentzos)** J.P. Larentzos, J.K. Brennan, J.D. Moore, and W.D. Mattson, "LAMMPS Implementation of Constant Energy Dissipative Particle Dynamics (DPD-E)", ARL-TR-XXXX, U.S. Army Research Laboratory, Aberdeen Proving Ground, MD.

## compute dpd/atom command

### Syntax:

```
compute ID group-ID dpd/atom
```

- ID, group-ID are documented in [compute](#) command
- dpd/atom = style name of this compute command

### Examples:

```
compute 1 all dpd/atom
```

### Description:

Define a computation that accesses the per-particle internal conductive energy (`u_cond`), internal mechanical energy (`u_mech`) and internal temperatures (`theta`) for each particle in a group. See the [compute dpd](#) command if you want the total internal conductive energy, the total internal mechanical energy, and average internal temperature of the entire system of dpd particles.

### Output info:

This compute calculates a per-particle array with 3 columns, which can be accessed by indices 1-3 by any command that uses per-particle values from a compute as input. See [Section howto 15](#) for an overview of LAMMPS output options.

The per-particle array values will be in energy and temperature [units](#) as discussed above.

### Restrictions:

The compute `dpd` is only available if LAMMPS is built with the appropriate USER-DPDE or USER-DPDE-SHARDLOW package.

### Related commands:

[compute dpd](#)

**Default:** none

---

(Larentzos) J.P. Larentzos, J.K. Brennan, J.D. Moore, and W.D. Mattson, "LAMMPS Implementation of Constant Energy Dissipative Particle Dynamics (DPD-E)", ARL-TR-XXXX, U.S. Army Research Laboratory, Aberdeen Proving Ground, MD.

## fix dpde command

### Syntax:

```
fix ID group-ID dpde
```

ID, group-ID are documented in [fix](#) command dpde = style name of this fix command

### Examples:

```
fix 1 all dpde
```

### Description:

Perform constant energy dissipative particle dynamics (DPD-E) integration to update position, velocity and internal energy for particles in the group at each timestep.

For fix *dpde*, the particle internal temperature is related to the particle internal energy through a mesoparticle equation of state. An additional fix must be specified that defines the equation of state for each particle.

---

### Restrictions:

The fix *dpde* is only available if LAMMPS is built with the appropriate USER-DPDE package.

The fix *dpde* requires the *dpd atom\_style* to be used in order to properly account for the particle internal energies and temperature.

The fix *dpde* must be used with an additional fix that specifies the mesoparticle equation of state for each particle.

### Related commands:

[fix nve](#) [fix eos/cv](#)

**Default:** none

---

(Larentzos) J.P. Larentzos, J.K. Brennan, J.D. Moore, and W.D. Mattson, "LAMMPS Implementation of Constant Energy Dissipative Particle Dynamics (DPD-E)", ARL-TR-XXXX, U.S. Army Research Laboratory, Aberdeen Proving Ground, MD.



## fix dpde/shardlow command

### Syntax:

```
fix ID group-ID dpde/shardlow
```

ID, group-ID are documented in [fix](#) command dpde/shardlow = style name of this fix command

### Examples:

```
fix 1 all dpde/shardlow
```

### Description:

Perform constant energy dissipative particle dynamics (DPD-E) integration using the Shardlow splitting algorithm (SSA) to update position, velocity and internal energy for particles in the group at each timestep. The SSA splits the integration into a stochastic and deterministic integration step. The stochastic integration of the dissipative and random forces is performed prior to the deterministic integration of the conservative force. Further details regarding the method are provided in [\(Lisal\)](#) and [\(Larentzos\)](#).

For fix *dpde/shardlow*, the particle internal temperature is related to the particle internal energy through a mesoparticle equation of state. An additional fix must be specified that defines the equation of state for each particle.

---

### Restrictions:

The fix *dpde/shardlow* is only available if LAMMPS is built with the appropriate USER-DPDE-SHARDLOW package.

The fix *dpde/shardlow* must be used with the *dpd/conservative* [pair\\_style](#) command to properly initialize pair coefficients for sigma and kappa.

The fix *dpde/shardlow* requires the *dpd* [atom\\_style](#) to be used in order to properly account for the particle internal energies and temperature.

The fix *dpde/shardlow* must be used with an additional fix that specifies the mesoparticle equation of state for each particle.

### Related commands:

[fix dpde](#) [fix eos/cv](#)

**Default:** none

---

**(Lisal)** M. Lisal, J.K. Brennan, J. Bonet Avalos, "Dissipative particle dynamics as isothermal, isobaric, isoenergetic, and isenthalpic conditions using Shardlow-like splitting algorithms.", J. Chem. Phys., 135, 204105 (2011).

**(Larentzos)** J.P. Larentzos, J.K. Brennan, J.D. Moore, M. Lisal and W.D. Mattson, "Parallel Implementation of Isothermal and Isoenergetic Dissipative Particle Dynamics Using Shardlow-Like Splitting Algorithms", Submitted to Comput. Phys. Commun., (2013).

**(Larentzos)** J.P. Larentzos, J.K. Brennan, J.D. Moore, and W.D. Mattson, "LAMMPS Implementation of Constant Energy Dissipative Particle Dynamics (DPD-E)", ARL-TR-XXXX, U.S. Army Research Laboratory, Aberdeen Proving Ground, MD.

## fix eos/cv command

### Syntax:

```
fix ID group-ID eos/cv cv
```

- ID, group-ID are documented in [fix](#) command
- eos/cv = style name of this fix command
- cv = constant-volume heat capacity

### Examples:

```
fix 1 all eos/cv 0.01
```

### Description:

Fix *eos/cv* applies a mesoparticle equation of state to relate the particle internal energy ( $u_i$ ) to the particle internal temperature ( $\theta_i$ ). The *eos/cv* mesoparticle equation of state requires the constant-volume heat capacity, and is defined as follows:

$$u_i = u_i^{mech} + u_i^{cond} = C_V \theta_i$$

where  $C_V$  is the constant-volume heat capacity,  $u_{cond}$  is the internal conductive energy, and  $u_{mech}$  is the internal mechanical energy. Note that alternative definitions of the mesoparticle equation of state are possible, but not currently implemented.

---

### Restrictions:

The fix *eos/cv* is only available if LAMMPS is built with the appropriate USER-DPDE or USER-DPDE-SHARDLOW packages.

The fix *eos/cv* must be used with the atom style *dpd*.

### Related commands:

[fix dpde](#)

**Default:** none

---

(Larentzos) J.P. Larentzos, J.K. Brennan, J.D. Moore, and W.D. Mattson, "LAMMPS Implementation of Constant Energy Dissipative Particle Dynamics (DPD-E)", ARL-TR-XXXX, U.S. Army Research Laboratory, Aberdeen Proving Ground, MD.

## pair\_style dpde command

### Syntax:

```
pair_style dpde kappa_flag cutoff seed
```

- kappa\_flag = 0/1 to turn off/on the energy-dependence of kappa (integer)
- cutoff = global cutoff for DPD interactions (distance units)
- seed = random # seed (positive integer)

### Examples:

```
pair_style dpde 0 2.5 34387
pair_style dpde 1 2.5 34387
pair_coeff * * 3.0 1.0 1.0 1.0
pair_coeff 1 1 3.0 1.0 1.0 1.0
```

### Description:

Style *dpde* computes a force field for dissipative particle dynamics (DPD) under isoenergetic conditions. The force on atom I due to atom J is given as a sum of 3 terms:

$$\begin{aligned}\vec{f} &= (F^C + F^D + F^R)\hat{r}_{ij} & r_{ij} < r_c \\ F^C &= A\omega_{ij} \\ F^D &= -\gamma\omega_{ij}^2(\hat{r}_{ij} \bullet \vec{v}_{ij}) \\ F^R &= \sigma_{ij}\omega_{ij}\zeta_{ij}(\Delta t)^{-1/2}\end{aligned}$$

where  $F^C$  is a conservative force,  $F^D$  is a dissipative force, and  $F^R$  is a random force.  $\hat{r}_{ij}$  is a unit vector in the direction  $\mathbf{r}_i - \mathbf{r}_j$ ,  $\mathbf{v}_{ij}$  is the vector difference in velocities of the two atoms =  $\mathbf{v}_i - \mathbf{v}_j$ ,  $\zeta$  is a Gaussian random number with zero mean and unit variance, and  $\Delta t$  is the timestep size.  $\gamma$  is set equal to  $(\sigma^2\sigma^2) / (2 K_B \Theta)$ , where  $K_B$  is the Boltzmann constant and  $\Theta$  is the particle internal temperature.

For style *dpde*, the weighting factor,  $\omega_{ij}$ , varies between 0 and 1, and is chosen to have the following functional form:

$$\omega_{ij} = 1 - \frac{r_{ij}}{r_c}$$

where  $r_c$  is the cutoff radius. Note that alternative definitions of the weighting function exist, but would have to be implemented with a separate pair style command.

The  $\omega_{ij}$  variable can be specified with or without an energy dependence by toggling the  $\kappa_{ij}$  flag. In the energy-independent model ( $\kappa_{ij} = 0$ ),  $\omega_{ij}$  is explicitly given as a pair coefficient. In the energy-dependent model ( $\kappa_{ij} = 1$ ),  $\omega_{ij}$  is given by the equation:

pair\_style dpde command

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$$\kappa_{ij} = \frac{\kappa_0}{k_B} \left( \frac{u_i + u_j}{2} \right)^2$$

where  $\kappa_0$  is the pair coefficient that is specified in the input file,  $k_B$  is the Boltzmann constant, and  $u_i$  is the total internal energy of particle  $i$ .

The differential internal conductive and mechanical energies are computed as

$$\begin{aligned} du_i^{cond} &= \kappa_{ij} \left( \frac{1}{\theta_i} - \frac{1}{\theta_j} \right) \omega_{ij}^2 + \alpha_{ij} \omega_{ij} \zeta_{ij}^q (\Delta t)^{-1/2} \\ du_i^{mech} &= -\frac{1}{2} \gamma_{ij} \omega_{ij}^2 \left( \frac{\vec{r}_{ij}}{r_{ij}} \bullet \vec{v}_{ij} \right)^2 - \frac{\sigma_{ij}^2}{4} \left( \frac{1}{m_i} + \frac{1}{m_j} \right) \omega_{ij}^2 - \frac{1}{2} \sigma_{ij} \omega_{ij} \left( \frac{\vec{r}_{ij}}{r_{ij}} \bullet \vec{v}_{ij} \right) \zeta_{ij} (\Delta t)^{-1/2} \end{aligned}$$

where

$$\begin{aligned} \alpha_{ij}^2 &= 2k_B \kappa_{ij} \\ \sigma_{ij}^2 &= 2\gamma_{ij} k_B \Theta_{ij} \\ \Theta_{ij}^{-1} &= \frac{1}{2} \left( \frac{1}{\theta_i} + \frac{1}{\theta_j} \right) \end{aligned}$$

$\zeta_{ij}$  is a second Gaussian random number with zero mean and unit variance that is used to compute the internal conductive energy.

For style *dpde*, the pairwise energy associated with style *dpde* is only due to the conservative force term  $F_c$ , and is shifted to be zero at the cutoff distance  $R_c$ . The pairwise virial is calculated using only the conservative term.

For style *dpde*, the following coefficients must be defined for each pair of atom types via the `pair_coeff` command as in the examples above, or in the data file or restart files read by the `read_data` or `read_restart` commands:

- A (force units)
- sigma (force\*time<sup>1/2</sup> units)
- kappa\_ij (energy\*temperature/time units) or kappa0 (1/time units)
- cutoff (distance units)

The last coefficient is optional. If not specified, the global DPD cutoff is used. Note that gamma is set equal to sigma\*sigma/(2 Theta), where Theta is the average internal temperature of the pair.

---

#### Mixing, shift, table, tail correction, restart info:

The pair style does not support mixing. Thus, coefficients for all I,J pairs must be specified explicitly.

The pair style does not support the `pair_modify` shift option for the energy of the pair interaction. Note that as discussed above, the energy due to the conservative  $F_c$  term is already shifted to be 0.0 at the cutoff distance  $R_c$ .

pair\_style dpde command

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The pair\_modify table option is not relevant for this pair style.

The pair style does not support the pair\_modify tail option for adding long-range tail corrections to energy and pressure.

The pair style writes its information to binary restart files, so `pair_style` and `pair_coeff` commands do not need to be specified in an input script that reads a restart file. Note that the user-specified random number seed is stored in the restart file, so when a simulation is restarted, each processor will re-initialize its random number generator the same way it did initially. This means the random forces will be random, but will not be the same as they would have been if the original simulation had continued past the restart time.

---

#### Restrictions:

The pair style *dpde* is only available if LAMMPS is built with the USER-DPDE or USER-DPDE-SHARDLOW package.

This pair style *dpde* requires the dpd atom style to be used in order to properly account for the particle internal energies and temperature.

This pair style *dpde* requires you to use the communicate vel yes option so that velocities are stored by ghost atoms.

#### Related commands:

pair\_coeff, pair\_dpd, fix dpde

**Default:** none

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(**Larentzos**) J.P. Larentzos, J.K. Brennan, J.D. Moore, M. Lisal and W.D. Mattson, "Parallel Implementation of Isothermal and Isoenergetic Dissipative Particle Dynamics Using Shardlow-Like Splitting Algorithms", Submitted to Comput. Phys. Commun., (2013).

(**Larentzos**) J.P. Larentzos, J.K. Brennan, J.D. Moore, and W.D. Mattson, "LAMMPS Implementation of Constant Energy Dissipative Particle Dynamics (DPD-E)", ARL-TR-XXXX, U.S. Army Research Laboratory, Aberdeen Proving Ground, MD.

## pair\_style dpde/conservative command

### Syntax:

```
pair_style dpde/conservative kappa_flag cutoff seed
```

- kappa\_model = 0/1 to turn off/on the energy-dependence of kappa (integer)
- cutoff = global cutoff for DPD interactions (distance units)
- seed = random # seed (positive integer)

### Examples:

```
pair_style dpde/conservative 0 2.5 34387
pair_style dpde/conservative 1 2.5 34387
pair_coeff * * 3.0 1.0 1.0 1.0
pair_coeff 1 1 3.0 1.0 1.0 1.0
```

### Description:

Style *dpde/conservative* computes the conservative force for dissipative particle dynamics (DPD). The conservative force on atom I due to atom J is given by

$$F^C = A\omega_{ij} \quad r_{ij} < r_c$$

where the weighting factor varies between 0 and 1, and is chosen to have the following functional form:

$$\omega_{ij} = 1 - \frac{r_{ij}}{r_c}$$

where  $\mathbf{R}_{ij}$  is a unit vector in the direction  $\mathbf{R}_i - \mathbf{R}_j$ , and  $R_c$  is the cutoff. Note that alternative definitions of the weighting function exist, but would have to be implemented with a separate pair style command.

The kappa\_ij variable can be specified with or without an energy dependence by toggling the kappa\_flag. In the energy-independent model (kappa\_flag = 0), kappa\_ij is explicitly given as a pair coefficient. In the energy-dependent model (kappa\_flag = 1), kappa\_ij is given by the equation:

$$\kappa_{ij} = \frac{\kappa_0}{k_B} \left( \frac{u_i + u_j}{2} \right)^2$$

where kappa0 is the pair coefficient that is specified in the input file, kB is the Boltzmann constant, and u\_i is the total internal energy of particle I.

This pair style differs from the other dpd styles in that the dissipative and random forces are not computed within the pair style. This style is combined with the fix *dpde/shardlow*, which will perform the stochastic integration of the dissipative and random forces through the Shardlow splitting algorithm approach.

For style *dpde/conservative*, the pairwise energy associated with style *dpde/conservative* is only due to the conservative force term  $F_c$ , and is shifted to be zero at the cutoff distance  $R_c$ . The pairwise virial is calculated

pair\_style dpde/conservative command

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using only the conservative term.

For style *dpde/conservative*, the following coefficients must be defined for each pair of atoms types via the `pair_coeff` command as in the examples above, or in the data file or restart files read by the `read_data` or `read_restart` commands:

- A (force units)
- sigma (force\*time<sup>1/2</sup> units)
- kappa\_ij (energy\*Temperature/time units) or kappa0 (1/time units)
- cutoff (distance units)

The last coefficient is optional. If not specified, the global DPD cutoff is used. Note that gamma is set equal to sigma\*sigma/(2 Theta), where Theta is the average internal temperature for the pair.

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#### Mixing, shift, table, tail correction, restart info:

The pair style does not support mixing. Thus, coefficients for all I,J pairs must be specified explicitly.

The pair style does not support the `pair_modify` shift option for the energy of the pair interaction. Note that as discussed above, the energy due to the conservative Fc term is already shifted to be 0.0 at the cutoff distance Rc.

The `pair_modify` table option is not relevant for these pair styles.

The pair style does not support the `pair_modify` tail option for adding long-range tail corrections to energy and pressure.

The pair style writes its information to binary restart files, so `pair_style` and `pair_coeff` commands do not need to be specified in an input script that reads a restart file. Note that the user-specified random number seed is stored in the restart file, so when a simulation is restarted, each processor will re-initialize its random number generator the same way it did initially. This means the random forces will be random, but will not be the same as they would have been if the original simulation had continued past the restart time.

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#### Restrictions:

The pair style *dpde/conservative* is only available if LAMMPS is built with the USER-DPDE-SHARDLOW package.

The pair style *dpde/conservative* requires the `dpd atom_style` to be used in order to properly account for the particle internal energies and temperature.

The pair style *dpde/conservative* requires you to use the `communicate vel yes` option so that velocities are stored by ghost atoms.

The pair style *dpde/conservative* will not restart exactly when using the `read_restart` command, though they should provide statistically similar results. This is because the forces they compute depend on atom velocities. See the `read_restart` command for more details.

#### Related commands:

`pair_style dpde/conservative` command

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pair\_coeff, pair\_dpd, pair\_dpde, fix\_dpde/shardlow

**Default:** none

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**(Larentzos)** J.P. Larentzos, J.K. Brennan, J.D. Moore, M. Lisal and W.D. Mattson, "Parallel Implementation of Isothermal and Isoenergetic Dissipative Particle Dynamics Using Shardlow-Like Splitting Algorithms", Submitted to Comput. Phys. Commun., (2013).

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